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# Conditioning of Generative Adversarial Networks for Pore and Reservoir-Scale Models

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**Imperial College  
London**



**TOTAL**

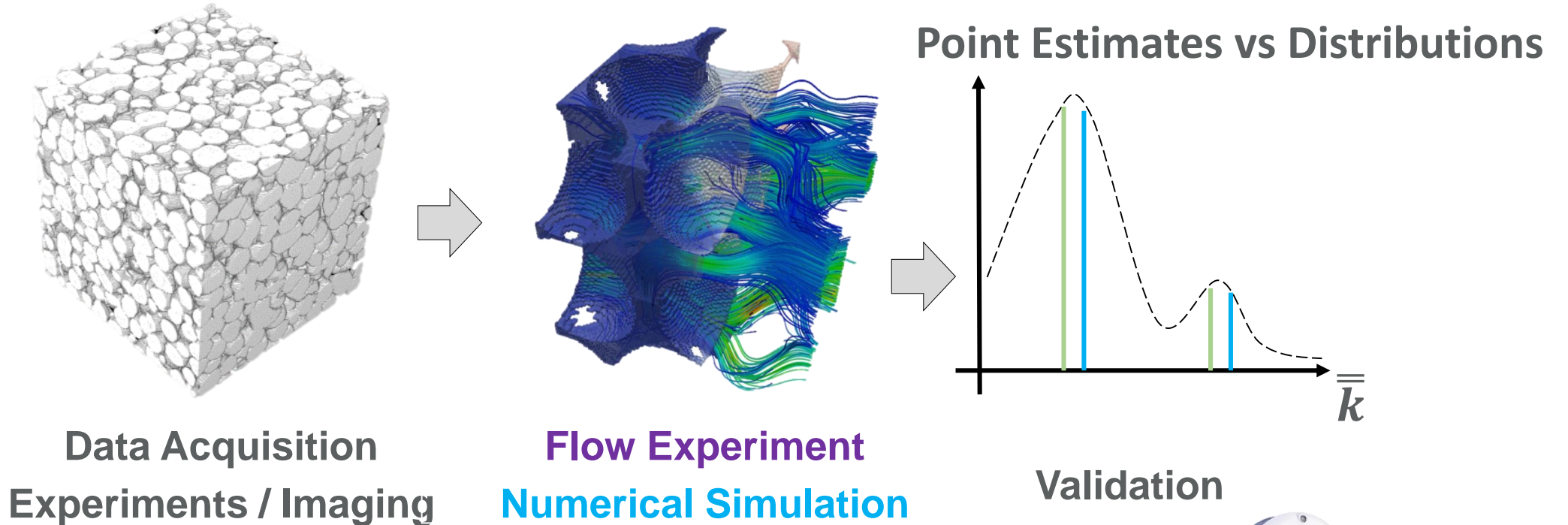
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# GANs in practice – Digital Rock and Core Physics



**Challenge:**  
How to quantify variability?

Perform measurements



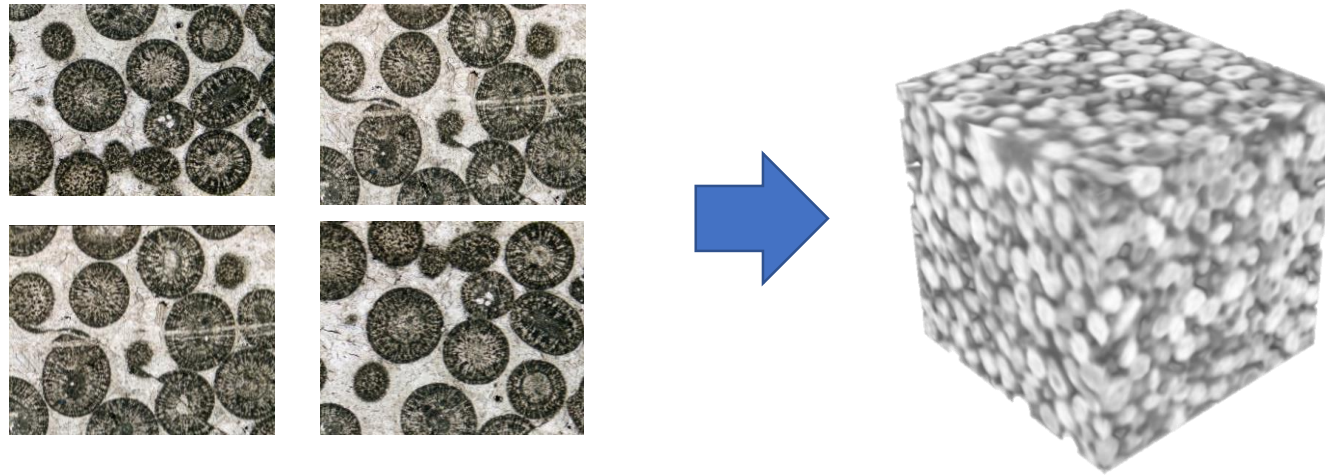
Generate Representative Images





# Why condition your generative model to data?

**Obtain a high-resolution 3D scan → condition 3D model to 2D sections**



**Thin sections more abundant / cheaper -> infer 3D structure**

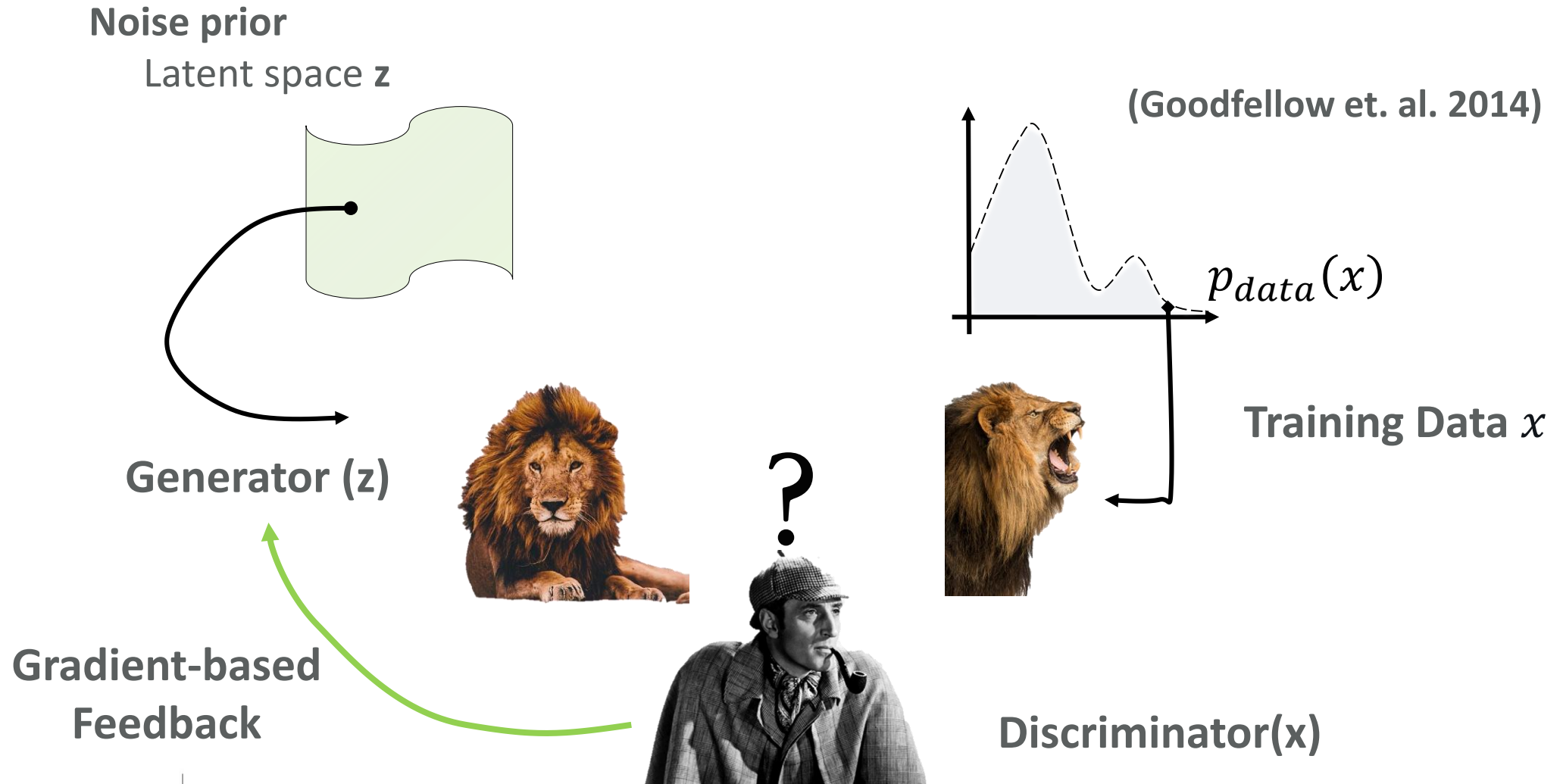
**Assists in experimental verification:**

- Keep same inflow geometry but vary 3D structure**

# Outline

- Generative Adversarial Networks
- Dataset – Ketton Limestone
- Validation of the Generative Model
  - Visual, Statistical and Physical Properties
- Conditioning to GANs to spatial data – pore and reservoir scale
- Where to from here?

# Generative Adversarial Networks – Toy Example



# Generative Adversarial Networks (Goodfellow et. al. 2014)

- **Task: Sample from unknown density, given by training samples / images**
- **Consist of two differentiable functions:**
  - **Generator  $G(z)$  and Discriminator  $D(x)$**
  - **$G(z)$  and  $D(x)$  represented by differentiable parametric (deep) neural networks**
- **Sample random noise  $z$  and apply function  $G(z)$  that maps to data domain e.g. images**
- **Two cost functions - competitive:**
  - **Discriminator  $D(x)$  goal: Distinguish real data from fake samples**
  - **Generator  $G(z)$  goal: Make samples look like data and fool discriminator**
  - **Convergence when discriminator confused therefore:**

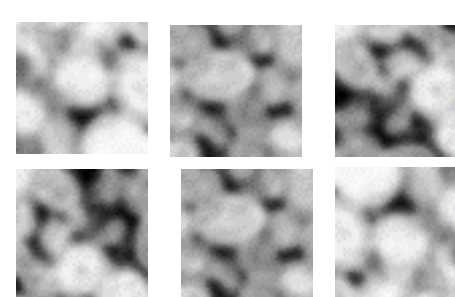
$$p_{data}(x) = p_{generated}(x)$$

**Allows very fast sampling (GPU optimized) of large 3D images**

# Ketton Limestone Dataset and Preprocessing

- **Oolitic Limestone**
- **Intergranular pores**
- **Intragranular Micro-Porosity**
- **Ellipsoidal grains**
- **99% Calcite**
- **Image Size:**
  - **$900^3$  voxels @  $26.7 \mu m$**

**Extract Non-Overlapping  
Training Images ( $64^3$  voxels)**

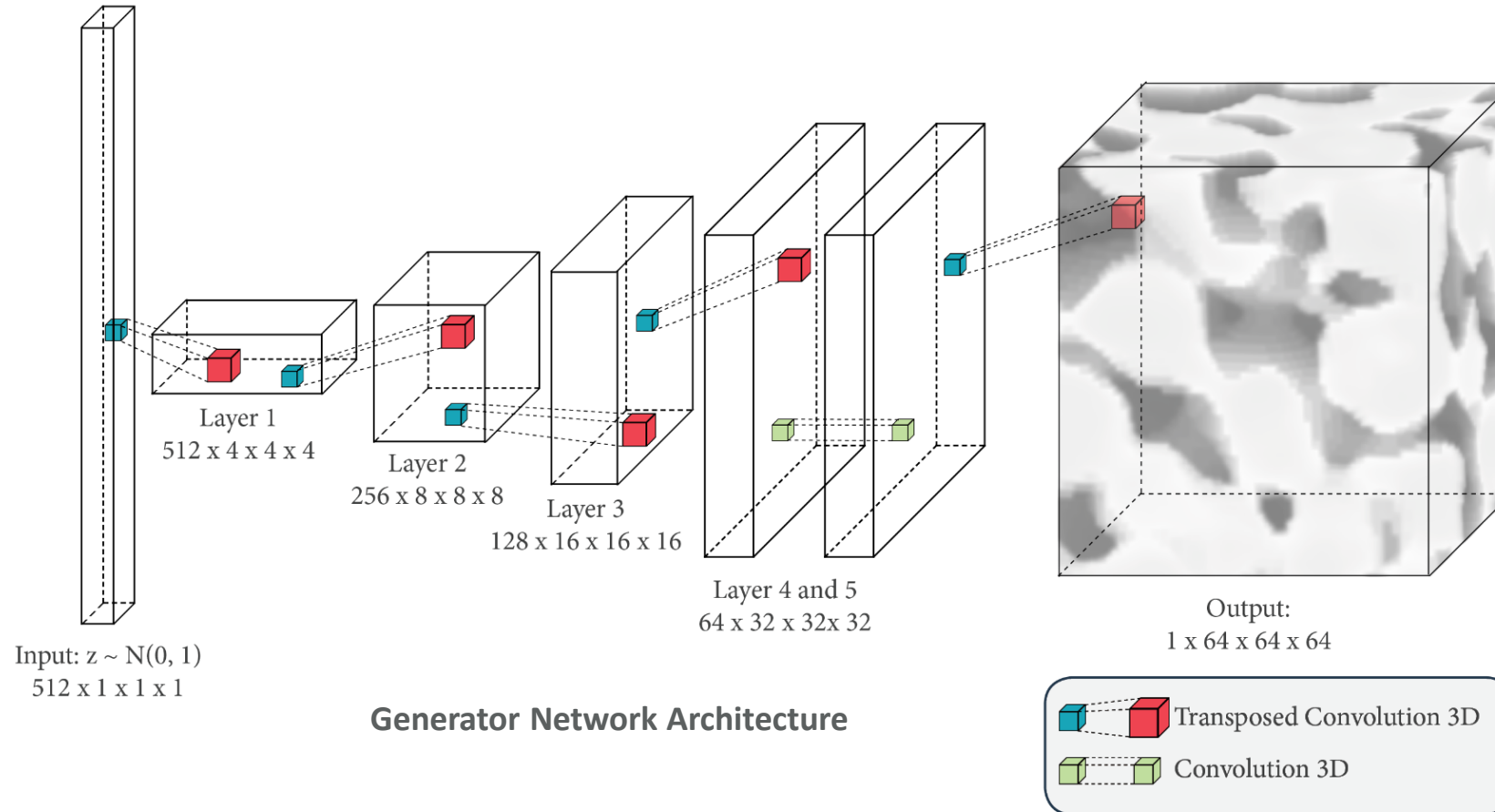


← **Training Set**



# Network Architecture – 3D Convolutional Network

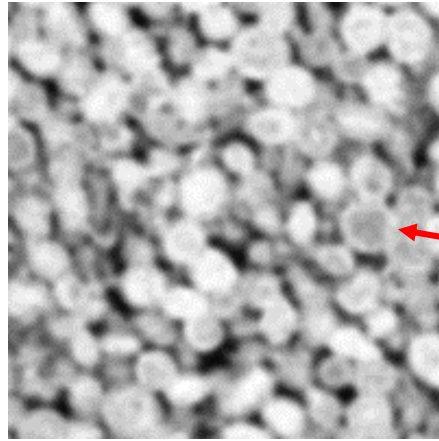
Represent  $G(z)$  and  $D(x)$  as deep neural networks:



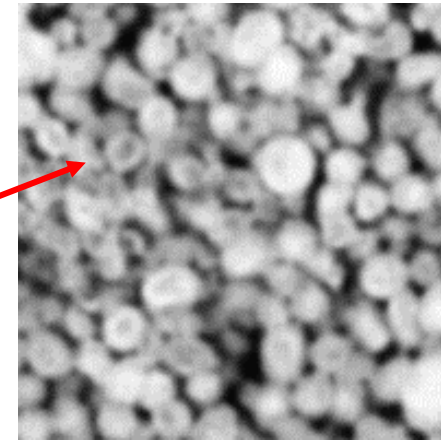
**Discriminator: Binary Classification Network -> Real / Fake**

# Reconstruction Quality – Unconditional Simulation

**Ketton Training Image**



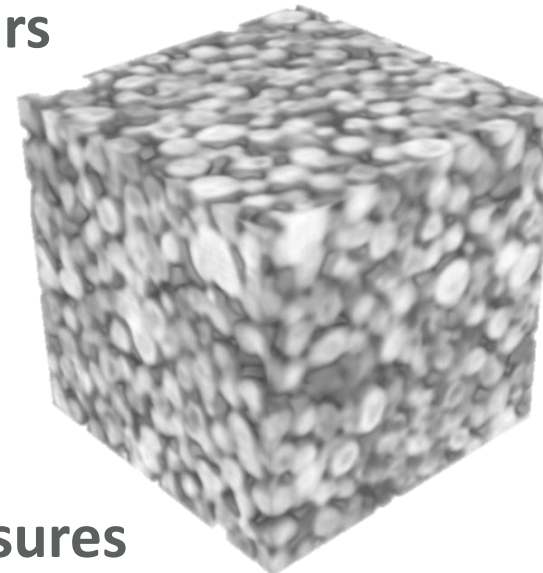
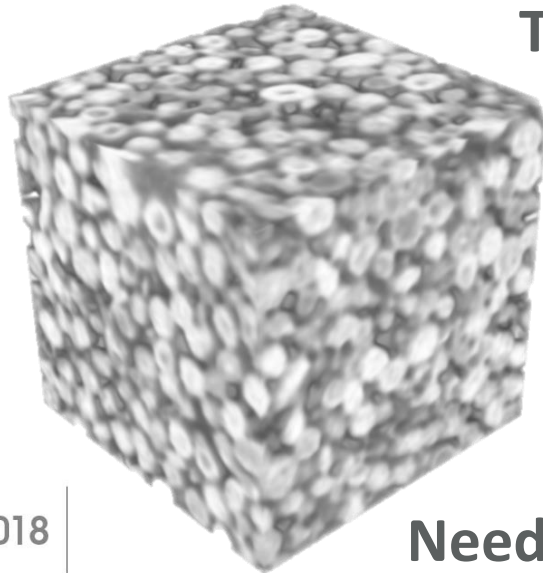
**GAN generated sample**



Intergranular Porosity  
Moldic Features  
Micro-Porosity

**Training Time: 8 hours**

**Generation: 5 sec**



**High visual quality**  
**Needs quantitative measures**

# Reconstruction Quality Criteria

## Statistical Properties

- **Two-Point Probability Function  $S_2(r)$** 
  - » Radial Average / Directional

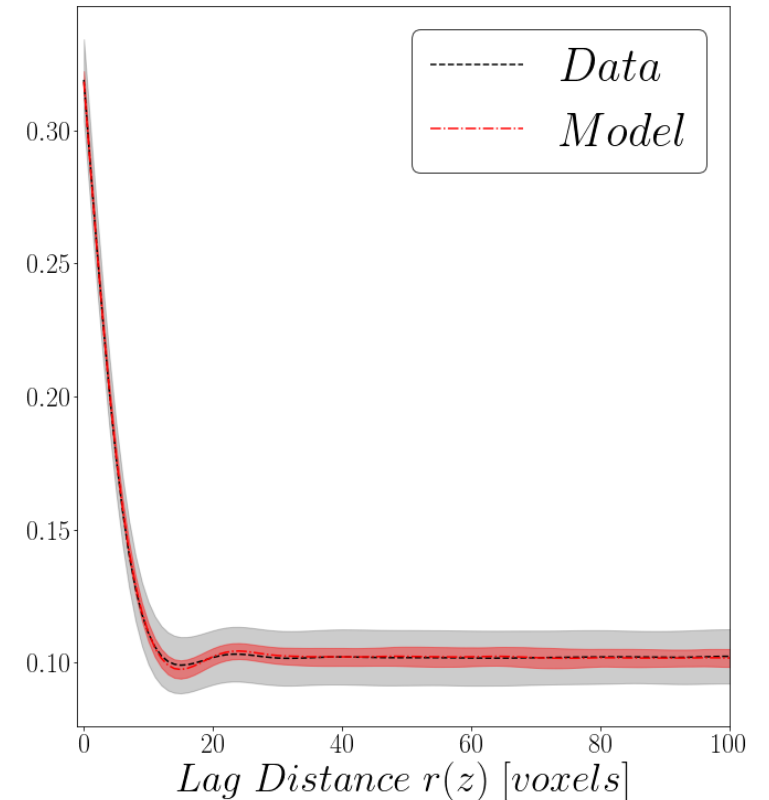
$$S_2(\mathbf{r}) = \mathbf{P}(\mathbf{x} \in P, \mathbf{x} + \mathbf{r} \in P) \text{ for } \mathbf{x}, \mathbf{r} \in \mathbb{R}^d$$

## Minkowski Functionals

- Porosity  $\phi$
- Specific Surface Area  $S_v$
- Integral of Mean Curvature
- Specific Euler Characteristic  $\chi_v$
- Compute as function of image gray-level  
=> Characteristic Curves

**Flow Properties: Solve Stokes flow in pore domain**

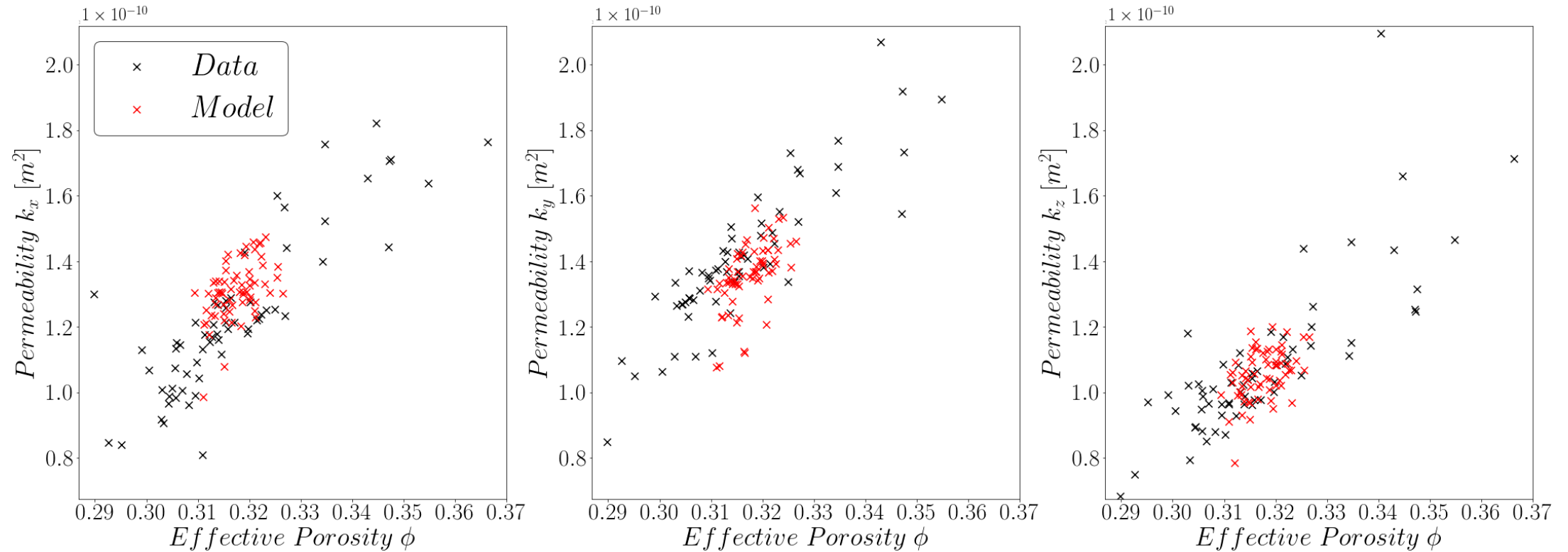
- Permeability + Velocity Distributions



$$\nabla \cdot \mathbf{v} = 0$$

$$\mu \nabla^2 \mathbf{v} = \nabla p$$

# Ketton Comparison – Permeability



## Isotropic Permeability

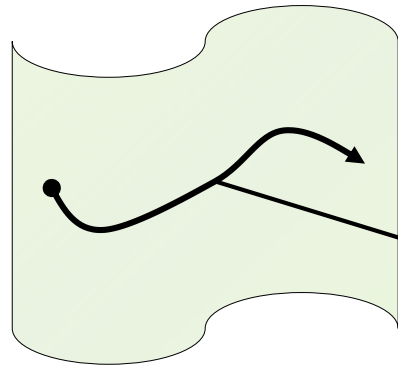
Range of effective (flowing) porosity: Data (0.29- 0.37) GAN (0.31-0.33)

Same order of magnitude and  $\bar{k} - \phi$  relationship

# Latent Space Interpolation

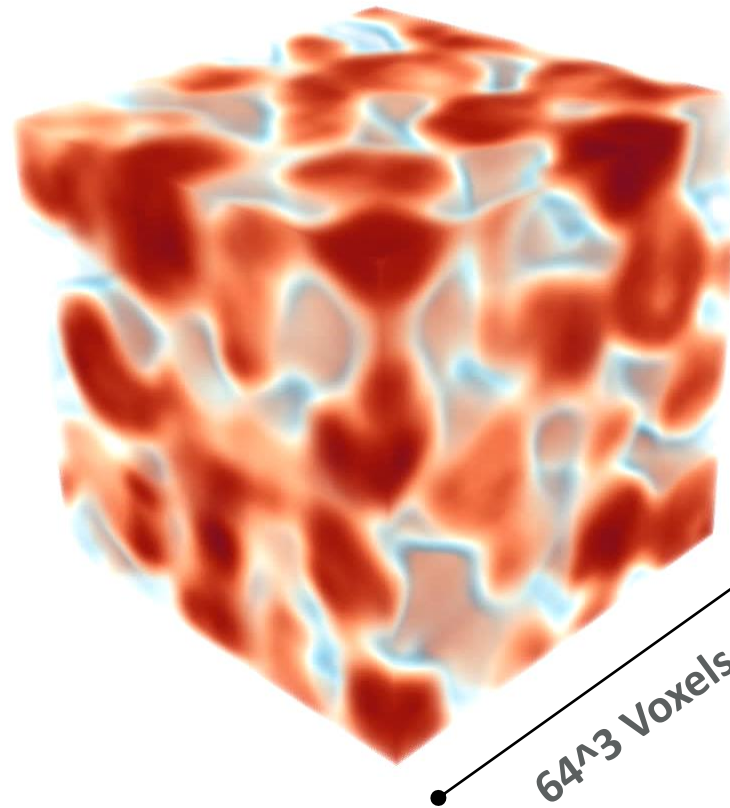
Latent space  $z$

$$z^* = \beta z_{start} + (1 - \beta) z_{end}, \beta \in [0, 1]$$



Interpolation path visualization

$G(z)$



**Interpolation in latent space:**

**Shows that generator has learned a meaningful representation in a lower dimensional space!**



# Generative Adversarial Networks are:

- **Generative Models**
- **Parametric – Latent Vector**
- **Differentiable – Allow for optimization (next part!)**
- **Paired – Generator (Sampling) and Discriminator (Evaluation)**

**They can be:**

- **Difficult to train – mode collapse and stability**
- **Difficult to evaluate – image quality and diversity**

**Once trained and qc'ed:**

- **Fast sampling**
- **Good computational scaling – with image size**
- **Load from Checkpoints - no need to start from scratch**

# Conditioning of Generative Models

Generative model should incorporate additional information:

e.g.  $G(z, \text{class}) \rightarrow \text{Sandstone, Shale, Carbonate}$

Train one generative model on images with associated class labels.

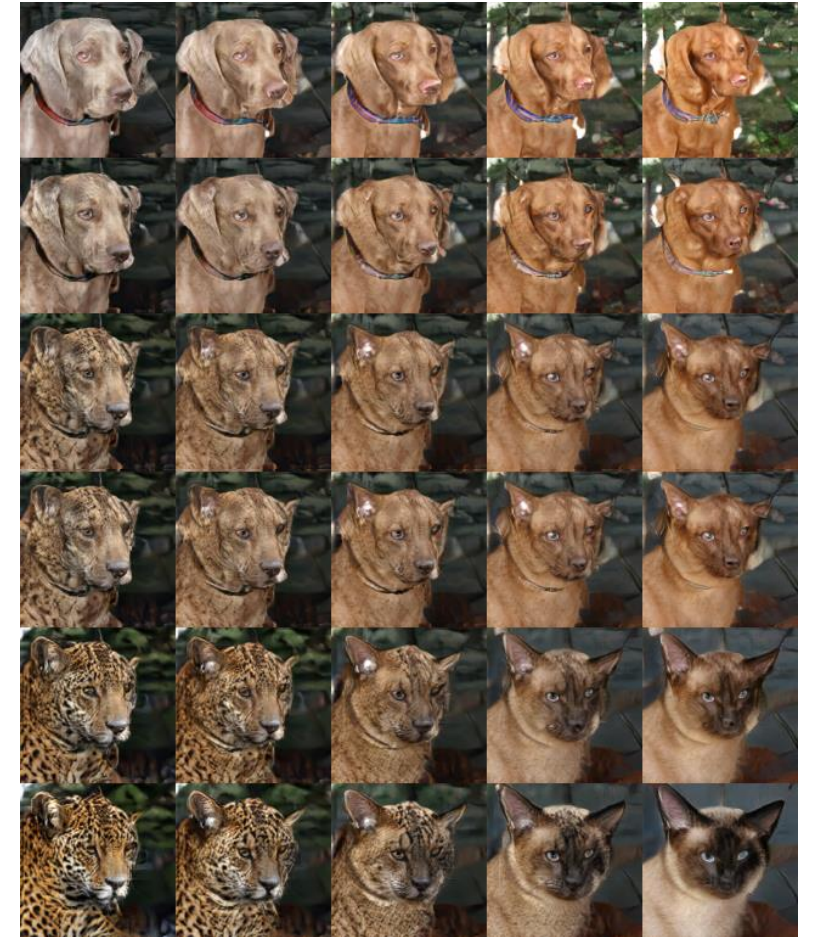
Generative model: Latent Vector + Class

Possible to perform smooth inter-class interpolation

E.g. Sand to shale to carbonate facies

This model  $\rightarrow$  Trained on Imagenet (1000 classes)

(Cat, Dog, Leopard, Dachshund)



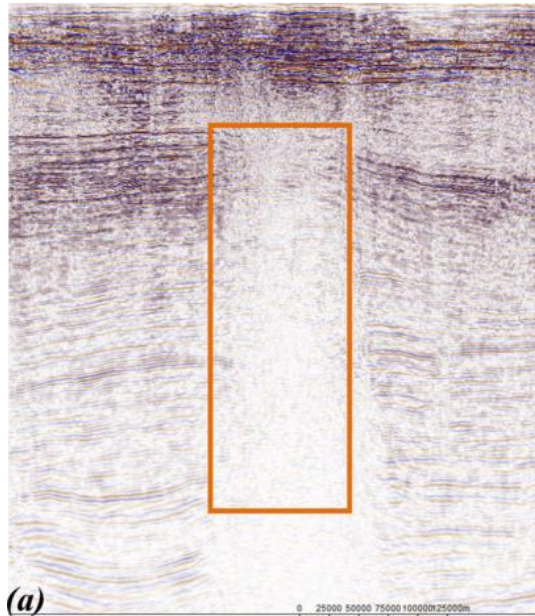
Miyato and Koyama 2018

# Conditioning of Generative Models

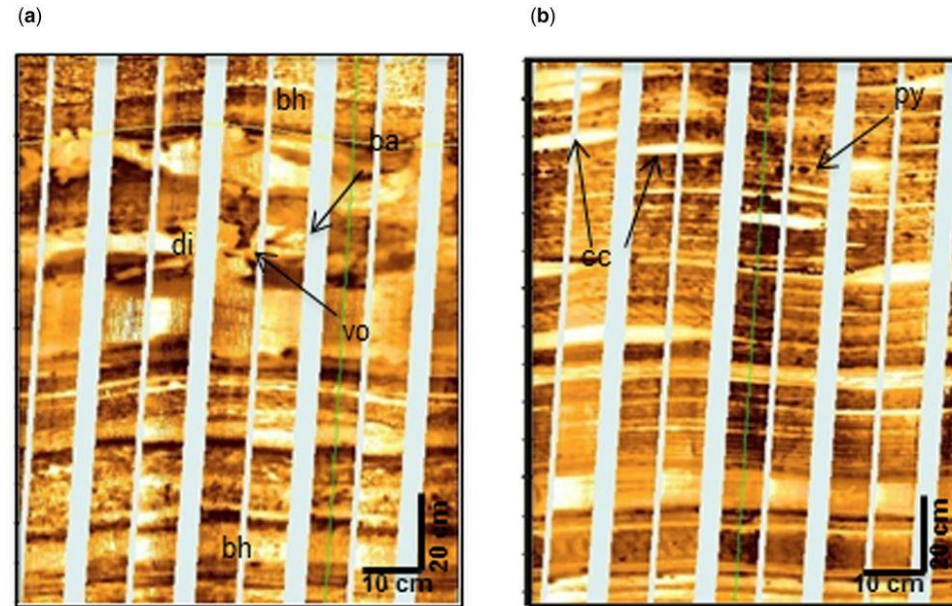
Individual samples should respect available **spatial** data:

Pore Scale: Thin Sections, FIB-SEM, Porosity, Rock Type

Reservoir Scale: Logs, Core Facies, Production Data, Seismic



Gas Chimney



Formation Micro-Imaging



# Image Inpainting (Yeh et al. 2016)

Task: Restore missing details given a corrupted / masked image  $M \cdot \tilde{x}$

Use a generative model  $G(z)$  to find missing details, conditional to given information.

Contextual Loss:  $L_{content} = \lambda ||M \cdot G(z) - M \cdot \tilde{x}||_2$   
Perceptual Loss:  $L_{perc} = \log(1 - D(G(z)))$  } Optimize loss by modifying latent vector  $z$



$M \cdot \tilde{x}$

Human Artist

$L_2$  Loss

$L_{content} + L_{perc}$

# Conditioning – Pore Scale Example

Two-dimensional data at pore-scale more abundant e.g. thin-sections  
Combine 3D generative model  $G(z)$  with 2D conditioning data

**Generative Model: Ketton Limestone GAN (Part 1)**

**Mask: Three orthogonal cross-sections, honor 2D data in a 3D image**

**Contextual Loss:**  $L_{content} = \lambda ||M \cdot G(z) - M \cdot \tilde{x}||_2$  on orthogonal cross-sections

**Perceptual Loss:**  $L_{perc} = \log(1 - D(G(z)))$  on whole volumetric generated image  $G(z)$

$$L_{Total} = \lambda L_{content} + L_{perceptual}$$

**Optimize Total Loss, by modifying latent vector (GAN parameters fixed)**

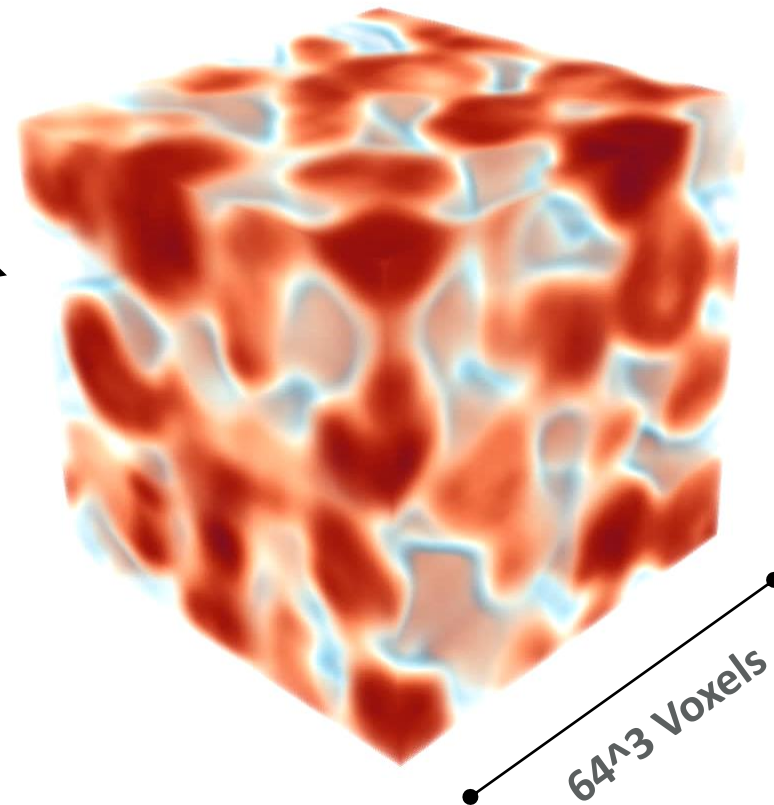
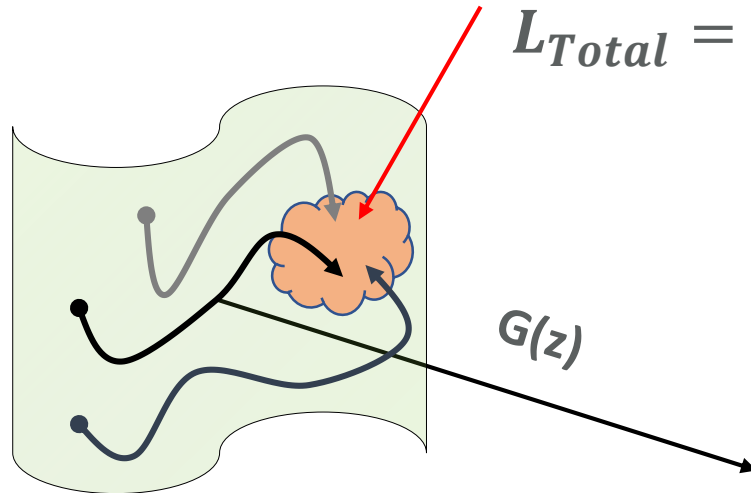
**-> Many local minima at error threshold -> stochastic volumes that honor 2D data**



# Conditioning Generative Networks

Traverse latent space by gradient-descent  
Subspace of all images that match the data

$$L_{Total} = \lambda L_{content} + L_{perceptual}$$



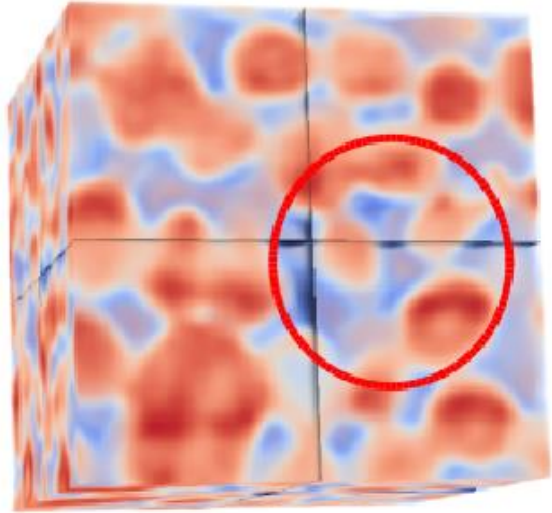
Latent space  $z$

Space of all valid unconditional images

Start from many random starting locations  
- > stochastic conditioned samples

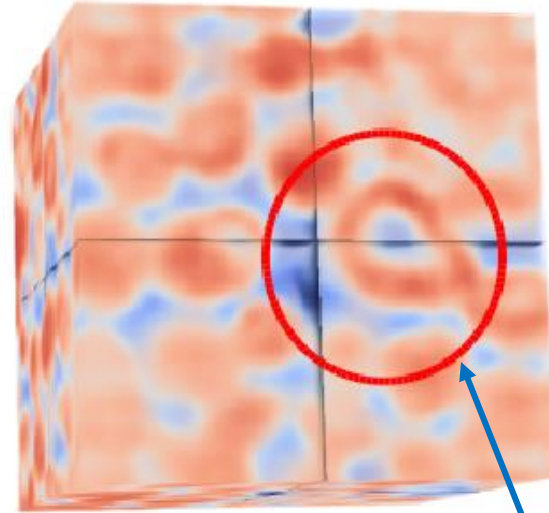
# Conditioning – Pore Scale Example

a)



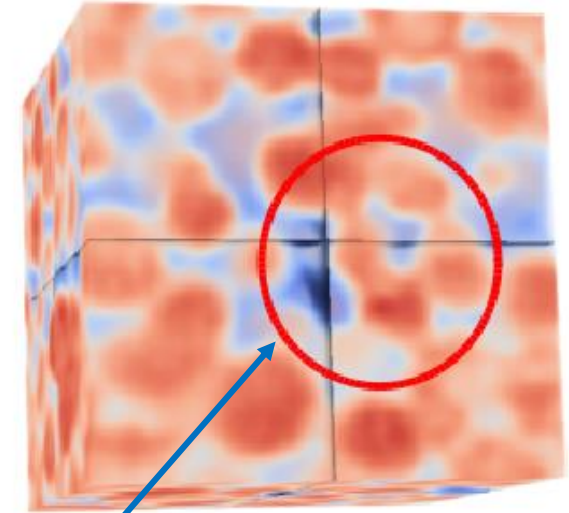
**Conditioning Data  
Ground Truth Volume**

b)



**Stochastic Sample 1  
Conditioned to Data**

c)



**Stochastic Sample 2  
Conditioned to Data**

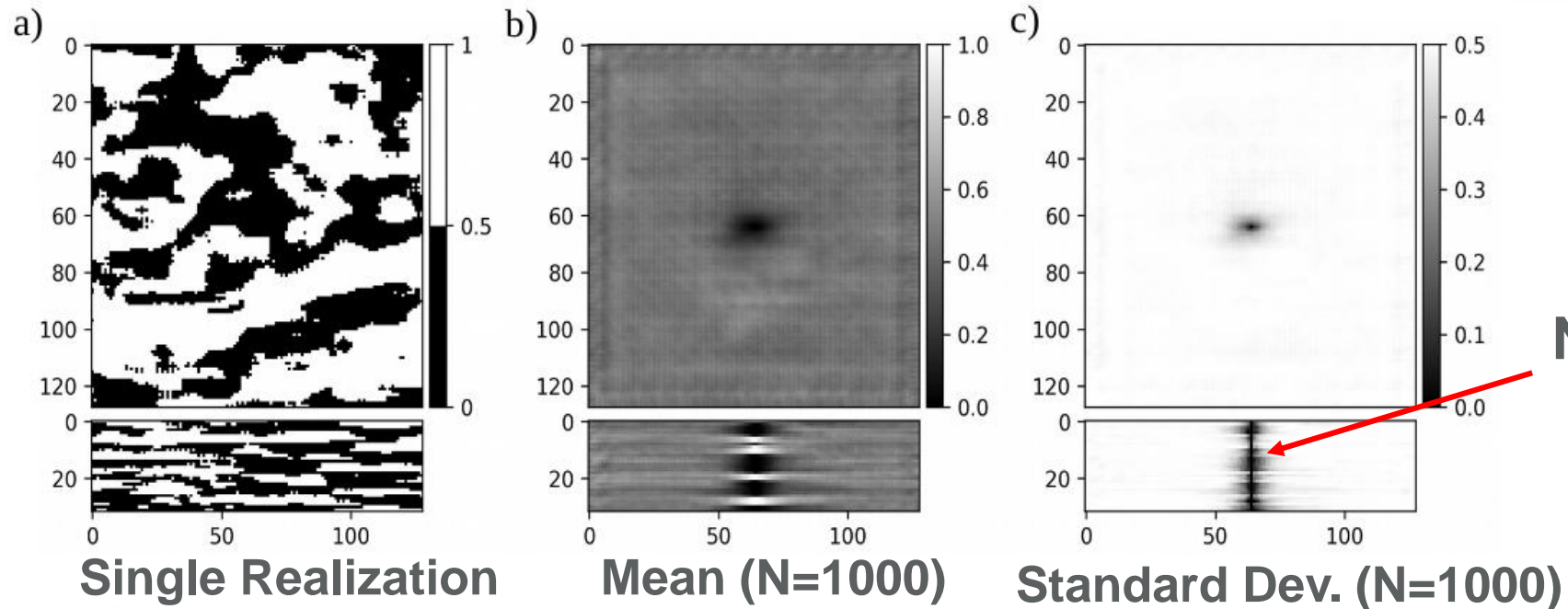
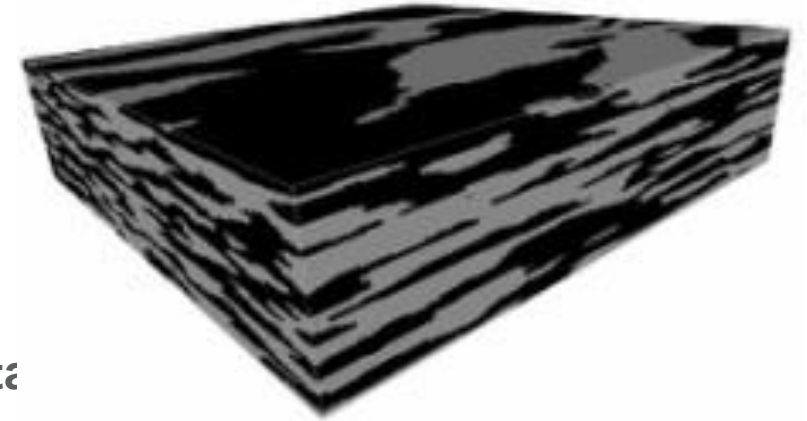
**Same 2D conditioning data leads to diverse realizations in 3D**

# Conditioning – Reservoir Scale Example

Maules Creek Training Image (Credit G. Mariethoz)

Pre-trained 3D-Generative Adversarial Network

Condition to single well (1D conditioning) from ground truth data:



No Variance at Well

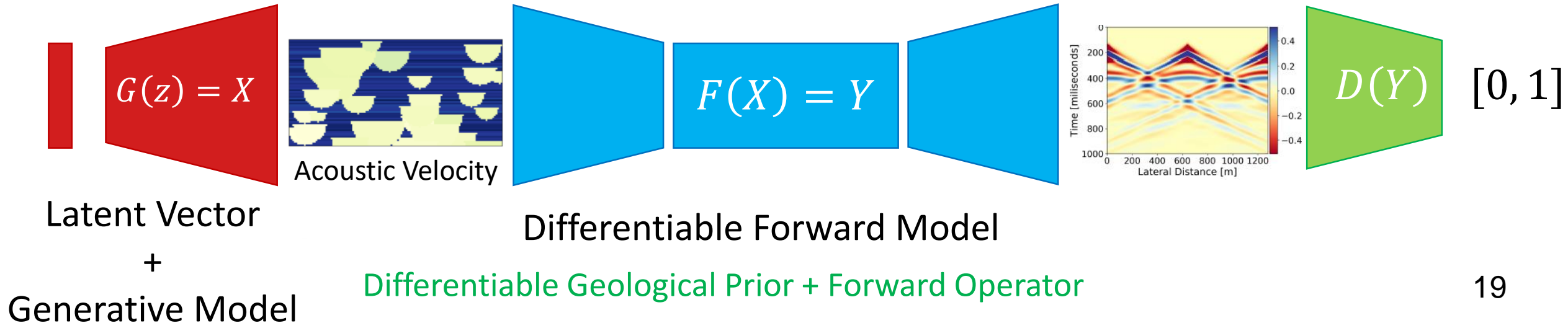
# GANs: A game changer for modeling and inversion?

## Summary:

- Stochastic Modeling using GANs at Pore and Reservoir Scale
- GANs provide flexible framework for conditioning to existing data – label and spatial data

## Many inverse problems could benefit from this:

- Reservoir Scale: Permeability derived from production data
- Seismic imaging: Acoustic/elastic properties from seismic data -> ArXiv Preprint





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**TOTAL**

Thank You!  
Questions?

Code on **GitHub** <https://github.com/LukasMosser/geogan>  
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